

# Reputation Systems II

Sybil Attack, BlogRank, B2Rank, EigenRumor,  
MailRank, TrustRunk

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# Outline

- 1 Sybil Attack
- 2 Ranking Blogs
- 3 Reputations For Fighting Spam
- 4 Conclusions

# 1

## Sybil Attack

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**Question:** whether splitting adversarial node into many is beneficial for acquiring higher reputation (rank)?

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**Answer:** double the graph.



# Positive Results (1/3)

General form of trust flow reputations:

$$r(x) = \max_{\mathcal{P}_{tx}} \bigoplus_{p \in \mathcal{P}_{tx}} \text{trust}(p)$$

Notation:

- $t$  is pre-trusted node
- $\mathcal{P}_{xy}$  is a family of disjoint paths from  $t$  to  $x$

# Positive Results (2/3)

Assumptions:

- 1 Extending path nonincreases the *trust*( $p$ )
- 2  $\oplus$  and *trust* are monotone to number of paths and edges values, respectively
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Proof?

# SybilGuard (1/2)

- Assume number of attack edges is  $A = o(\sqrt{n}/\log n)$
- System is distributed, honest nodes follow the same protocol
- Can an honest node  $t$  identify (w.h.p.)  $2A + 1$  nodes in such a way that at most  $A$  of them are powered by adversary?

## SybilGuard (2/2)

- For every node fix a bijective mapping from in-edges to out-edges
- Take a walk from  $t$  of length at most  $\sqrt{n} \log n$  using bijection routing
- At some point make a random switch, then continue another  $\sqrt{n} \log n$  steps using backwalk routing
- Report a point. Repeat, until  $2A + 1$  points are collected



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### Claim

w.h.p. at most  $A$  reported nodes are malicious

# 2

## Ranking Blogs

# Ranking Blogs: Factors

- Entities: blogs, posts, communities, comments, brand names, external websites
- Friends, blogroll, subscriptions, hyperlinks, visitors, clicks, votes
- Time
- Tags

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Wait a minute, for which graph? Linked blogs:

- Hyperlinks, blogrolls
- Common commentors/authors, tags, co-references to news

# B2Rank

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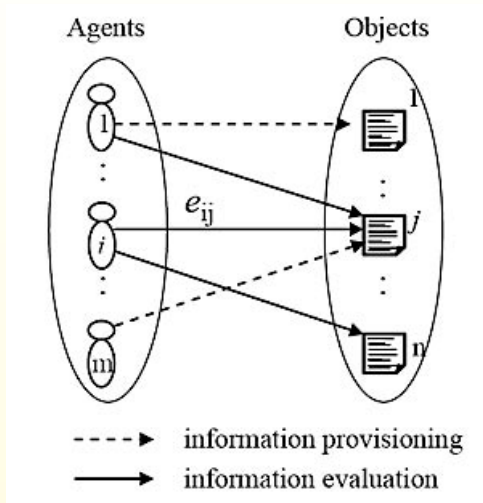
*BlogReputation* is computed in PageRank style for blogroll graph with one change:

- Blogroll links are weighted by activity level (frequency of blogging and commenting)

*PostQuality* is average for PageRank-style score of blog posts

- Post-to-post links are weighted by referring post activity and time difference

# EigenRumor (1/2)



# EigenRumor (2/2)

Notation:

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- $P, E$ : provision and evaluation matrices

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Solution: iterative algorithm for  $\bar{r}$ :

$$\bar{r} = (\alpha P^T P + (1 - \alpha) E^T E) \bar{r}$$

# 3

## Reputations For Fighting Spam

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- Compute reputations a-la PageRank

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## Conclusions



# Challenges

- Measurable objectives?
- Model for input data?
- Dynamic aspects of reputations?  
Digg-style ranking?
- Price of attack?
- Ranking in social networks?
- Ranking in RDF data?
- Billion dollar question: how to avoid arms race?

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Combating web spam with TrustRank



M. Dalal

Spam and popularity ratings for combating link spam

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<http://yury.name/reputation.html>

Ongoing project: <http://businessconsumer.net>

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Thanks for your attention!  
Questions?